

You can also solve triangles that are not right triangles using the *Law of Cosines*. There are three rules that make up the law of cosines, but you only need to memorize one because the other two can be obtained by changing the letters (put b in place of a , for example). All three rules are listed below.

$$a^2 = b^2 + c^2 - 2bc(\cos A)$$

$$b^2 = a^2 + c^2 - 2ac(\cos B)$$

$$c^2 = a^2 + b^2 - 2ab(\cos C)$$

The *law of cosines* can be used in two different cases. First, if you know the lengths of all three sides of a triangle, you can use the law of cosines. Secondly, you can use the law of cosines when two sides and the included angle are known.

Example:

1. Problem: In *triangle ABC*, $a = 24$,
 $c = 32$, and *angle B* = 115° .
 Solve the triangle.

Solution: We know two sides. Find the third using the law of cosines.

$$b^2 = a^2 + c^2 - 2ac(\cos B)$$

Plug in any known information.

$$b^2 = 24^2 + 32^2 - 2 * 24 * 32(-.4226)$$

$$b^2 = 2249$$

Solve for b by taking the square root of each side.

$$b = \text{SQRT}(2249) = 47.4$$

Using the law of sines,
 $\text{angle A} = 27.32^\circ$.

Since we know that triangles are made of three angles that sum to 180° , we can find the measure of *angle C* by setting up an equation.

$$\text{Angle C} = 180^\circ - 115^\circ - 27.32^\circ = 37.68^\circ$$

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