

The derivative of f at the number a is given by $f'(a) = \lim_{h \rightarrow 0} \frac{f(a+h) - f(a)}{h}$,
provided that this limit exists.

Example: (a) Find the derivative of $f(x) = x^2$ from first principles.

(b) And determine the slopes of the tangents to the parabola $y = x^2$ at $x = -2$

$$\begin{aligned} \text{(a)} \quad f'(x) &= \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} \\ &= \lim_{h \rightarrow 0} \frac{(x+h)^2 - x^2}{h} \\ &= \lim_{h \rightarrow 0} \frac{x^2 + 2hx + h^2 - x^2}{h} \\ &= \lim_{h \rightarrow 0} \frac{h(2x+h)}{h} \\ &= \lim_{h \rightarrow 0} (2x+h) \\ &= 2x \end{aligned}$$

$$\text{(b)} \quad f'(x) = 2x, \quad x = -2$$

$$f'(-2) = -4$$

The slopes is -4 at $x = -2$

Find the derivative of from first principles, given $f(x)$.

1) $f(x) = 3$	2) $f(x) = 4x$	3) $f(x) = 2x^3$
4) $f(x) = x^3 + 2x^2 + 1$	5) $f(x) = \sqrt{ax^2 + b}$	6) $f(x) = \frac{1}{\sqrt{3x}}$
7) $f(x) = \frac{x+1}{x-1}$	8) $f(x) = \frac{1}{x^3}$	9) $f(x) = 2x + \frac{1}{x^2}$

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